

Tutorial 3

Question 1

$$\begin{aligned} \text{a) } 4^8 \times 4^3 \\ &= 4^{8+3} \\ &= 4^{11} \end{aligned}$$

$$\begin{aligned} \text{b) } 6^4 \div 6^{-6} \\ &= 6^{4-(-6)} \\ &= 6^{10} \end{aligned}$$

$$\begin{aligned} \text{c) } (8^9)^{-3} \\ &= 8^{9 \times (-3)} \\ &= 8^{-27} \end{aligned}$$

Question 2.

$$\text{a) } \frac{9(x^2)^2}{3xy^2} = \frac{9x^4}{3xy^2}$$

$$= \frac{9}{3} \cdot \frac{x^4}{x} \cdot \frac{1}{y^2}$$

$$= 3x^{4-1} y^{-2}$$

$$= 3x^3 y^{-2}$$

$$= 3x^3 \left(\frac{1}{y^2}\right)$$

$$= \frac{3x^3}{y^2}$$

$$\text{b) } \frac{a \times (ab^4)^2}{(a^2 \times b)^3}$$

$$= \frac{a \times a^2 b^8}{a^6 \times b^3}$$

$$= \frac{a^{1+2} b^8}{a^6 b^3}$$

$$= \frac{a^3 b^8}{a^6 b^3}$$

$$= a^{3-6} b^{8-3}$$

$$= a^{-3} b^5$$

$$= \frac{1}{a^3} b^5$$

$$= \frac{b^5}{a^3}$$

Question 3

$$c) \frac{a^{-2}}{b^3} \div \left(\frac{a}{b^2}\right)^{-2}$$

$$= \frac{a^{-2}}{b^3} \div \left(\frac{a}{b^2}\right)^{-2}$$

$$= \frac{a^{-2}}{b^3} \cdot \frac{1}{a^2}$$

$$= \frac{a^{-2}}{b^3} \cdot \frac{b^4}{a^2}$$

$$= \frac{a^{-2}}{b^3} \times \frac{a^2}{b^4}$$

$$= \frac{a^{-2} \times a^2}{b^3 \times b^4}$$

$$= \frac{a^{-2+2}}{b^{3+4}}$$

$$= \frac{a^0}{b^7}$$

$$= \frac{1}{b^7}$$

$$a) 2^{7x} \cdot 2 = 258^x$$

$$2^{7x} \cdot 2^3 = 2^{8x}$$

$$7x + 3 = 8x$$

$$7x - 8x + 3 = 8x - 8x$$

$$-x + 3 = 0$$

$$-x + 3 - 3 = 0 - 3$$

$$= x = -3$$

$$\frac{-x}{-1} = \frac{-3}{-1}$$

$$x = 3$$

$$b) \left(\frac{1}{36}\right)^{3-x} \left(\frac{1}{6}\right)^x = 216$$

$$\left(\frac{1}{6^2}\right)^{3-x} \left(\frac{1}{6}\right)^x = 6^3$$

$$(6^{-2})^{3-x} (6^{-1})^x = 6^3$$

$$6^{-6+2x} 6^{-x} = 6^3$$

$$6^{-6+2x-x} = 6^3$$

$$-6 + 2x - x = 3$$

$$-6 + x$$

$$-6 + x = 3 + 6$$

$$x = 9$$