

Tutorial 2

Nama: Felester COSOOT17F2039

No.

Date

Question 1

Given that the Universal Set $E = \{x : 28 \leq x \leq 70, x \text{ is an integer}\}$

Set $L = \{x : x \text{ is a perfect square}\}$,

Set $M = \{x : x \text{ is a multiple of 4}\}$

Set $N = \{x : x \text{ is a number such that one of its digits is 2}\}$

(a) Sketch the Venn Diagram for the set E, L, M and N .

(b) Find all the elements of $n(M \cap N)$ and $n(L \cup M)$

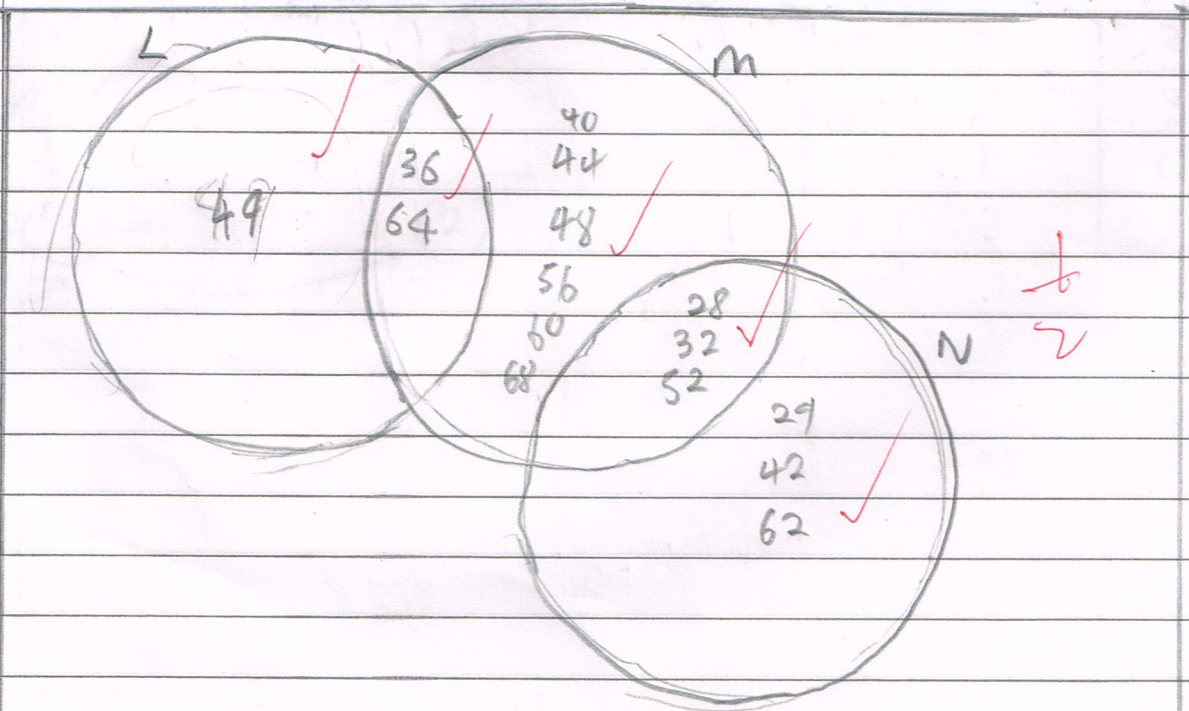
Answer:

a) $E = \{28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70\}$

$L = \{36, 49, 64\}$

$M = \{32, 36, 40, 44, 48, 52, 56, 60, 64, 68\}$

$N = \{28, 29, 32, 42, 52, 62\}$



b) $M \cap N = \{28, 32, 52\}$
 $n(M \cap N) = 3$

$L \cup M = \{28, 32, 52, 40, 44, 48, 68, 56, 60, 64, 36, 49\}$

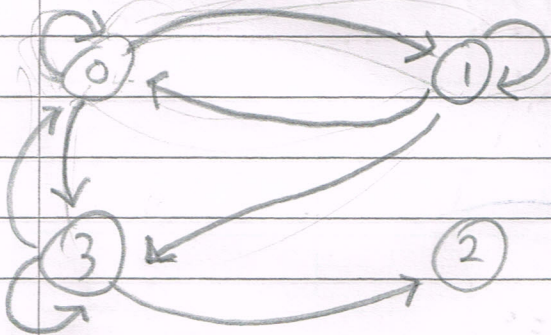
$n(L \cup M) = 12$

Question 2.

Given $A = \{0, 1, 2, 3\}$ and the relation R on A is defined as follows:

$R = \{(0, 0), (0, 1), (0, 3), (1, 0), (1, 1), (1, 3), (3, 0), (3, 2), (3, 3)\}$

a) Draw the directed graph of R relation.



	Indegree	outdegree
0	3	3
1	2	3
2	1	0
3	3	3

(6) Determine whether the given relation is equivalence on $\{0, 1, 2, 3\}$ or not by justifying your answer. $R = \{(1, 1), (1, 2), (2, 1), (2, 2)\}$

$\therefore R$ is not reflexive because the elements of $\{0, 1, 2, 3\}$ is not connected.

$= R$ is not symmetric because $3 R 2$ but $2 \not R 3$.

$= R$ is not transitive because $3 R 2$, $2 R 1$ but $3 \not R 1$.

$= R$ is not an Equivalence relation because R is not transitive and not reflexive.

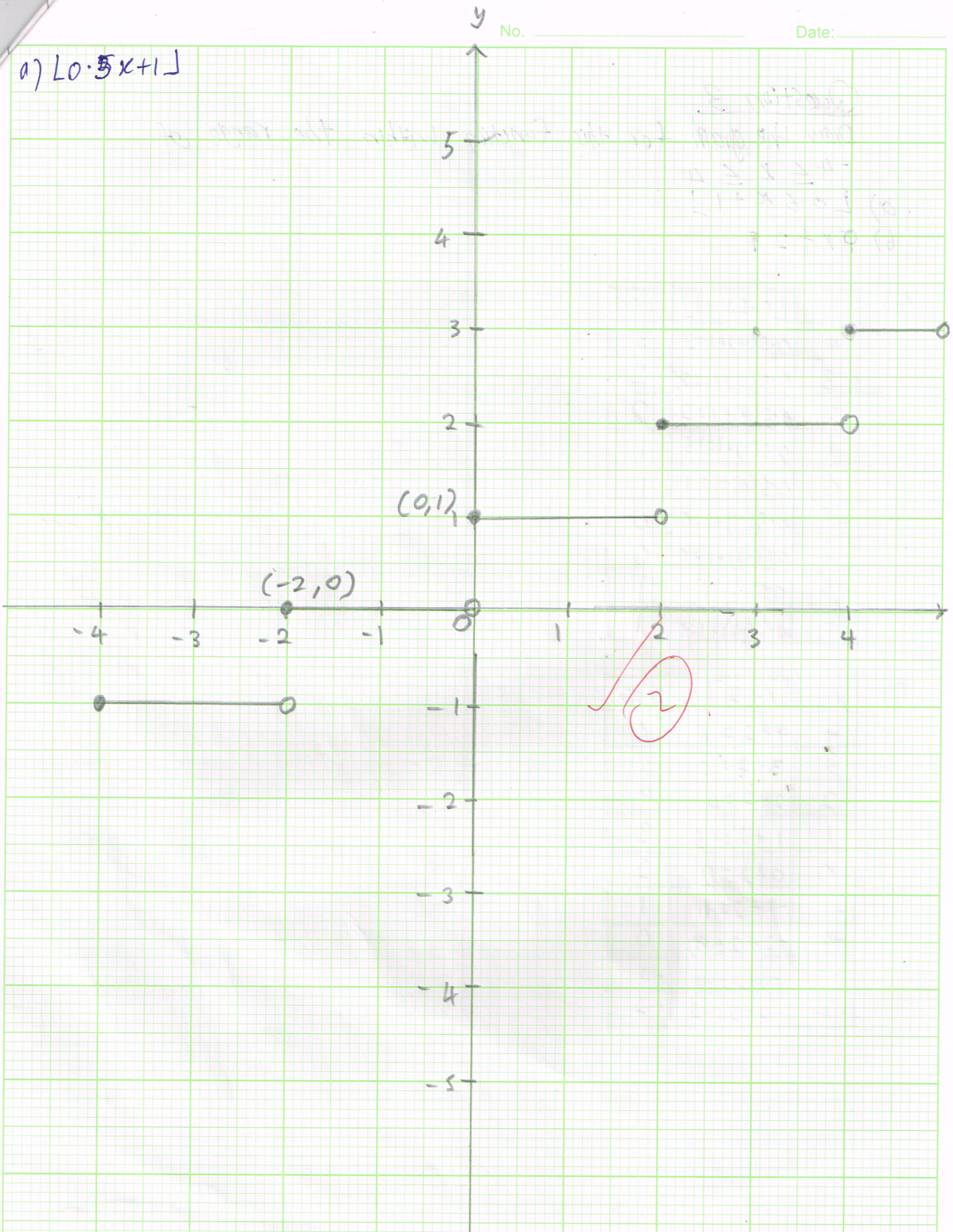
$\therefore R$ is not an Equivalence relation. *imp. qn.*

$(0, 0), (0, 1), (1, 1), (1, 0), (2, 2), (3, 3) = \{ (0, 0), (0, 1), (1, 1), (1, 0), (2, 2), (3, 3) \}$

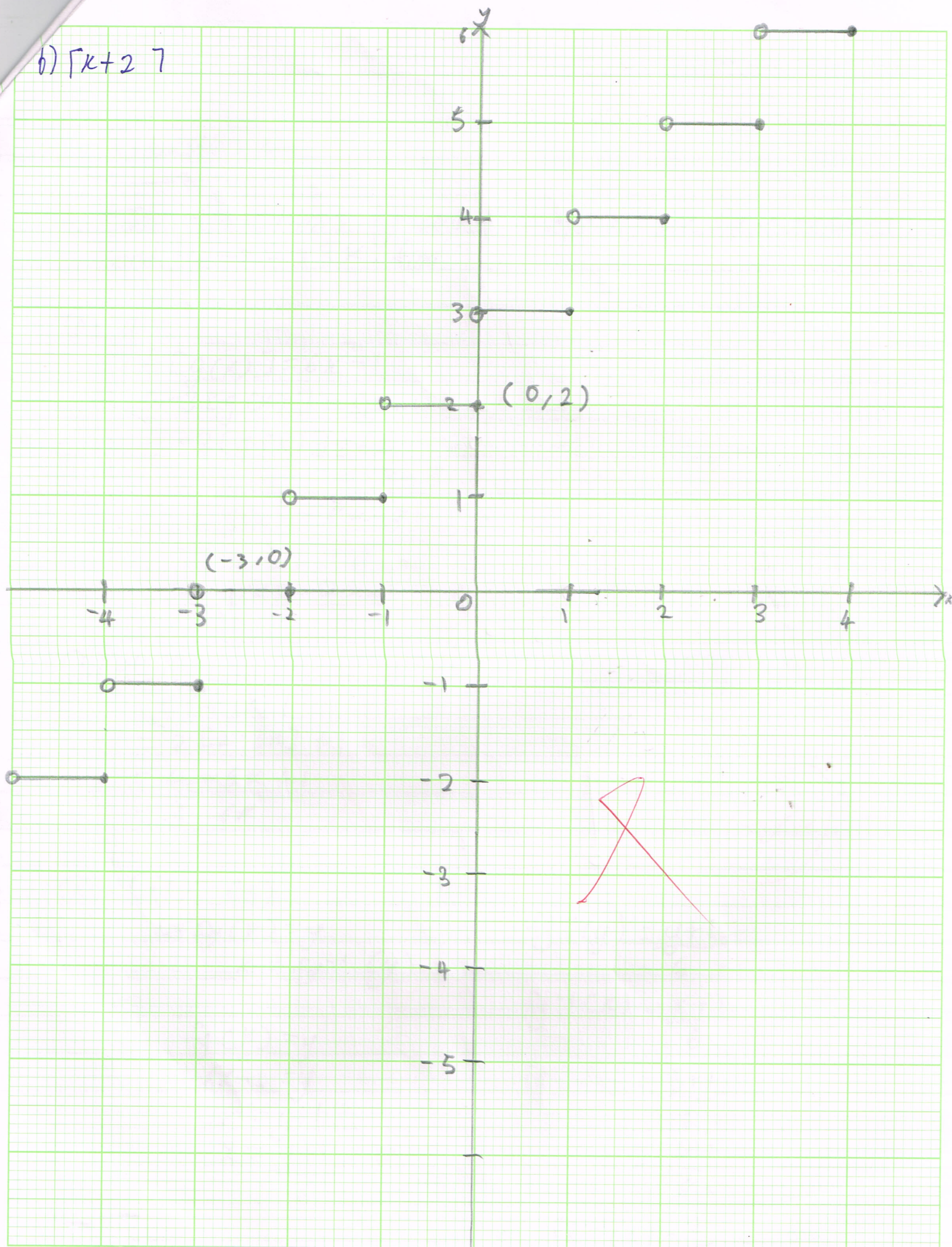
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a) $\lfloor 0.5x + 1 \rfloor$



b) $\lceil x+2 \rceil$



Question 4.

The functions fg and f are given by $fg: K \rightarrow 6K-1$ and $f: x \rightarrow 2-3x$. find:

(a) g

$$f[g(K)] = 6K-1$$

$$2-3[g(K)] = 6K-1$$

$$-3[g(K)] = 6K-1-2$$

$$= 6K-3$$

$$g(K) = \frac{6K-3}{-3}$$

$$g(K) = 2K+1$$

(b) gf

$$g[f(K)]$$

$$= 2[2-3K] + 1$$

$$= 4-6K+1$$

$$= 5-6K$$

(c) $(fg)^{-1}(3)$

$$\text{Let } fg(K) = y$$

$$K = fg^{-1}(y)$$

$$fg(K) = y$$

$$6K-1 = y$$

$$6K = y+1$$

$$K = \frac{y+1}{6}$$

$$fg^{-1}(y) = \frac{y+1}{6}$$

$$fg^{-1}(K) = \frac{K+1}{6}$$

$$fg^{-1}(3) = \frac{3+1}{6}$$

$$= \frac{4}{6}$$

$$fg^{-1}(3) = \frac{2}{3}$$

Tutorial 2 (Maths)

Name: Helary Laurine

DDT2B

05DDT17F 2003

Question 1

Given that the universal set $\{ = \{x : 28 \leq x \leq 70, x \text{ is an integer} \}$

Set $L = \{x : x \text{ is a perfect square} \}$

Set $M = \{x : x \text{ is a multiple of } 4 \}$

Set $N = \{x : x \text{ is a number such that one of its digit is } 2 \}$

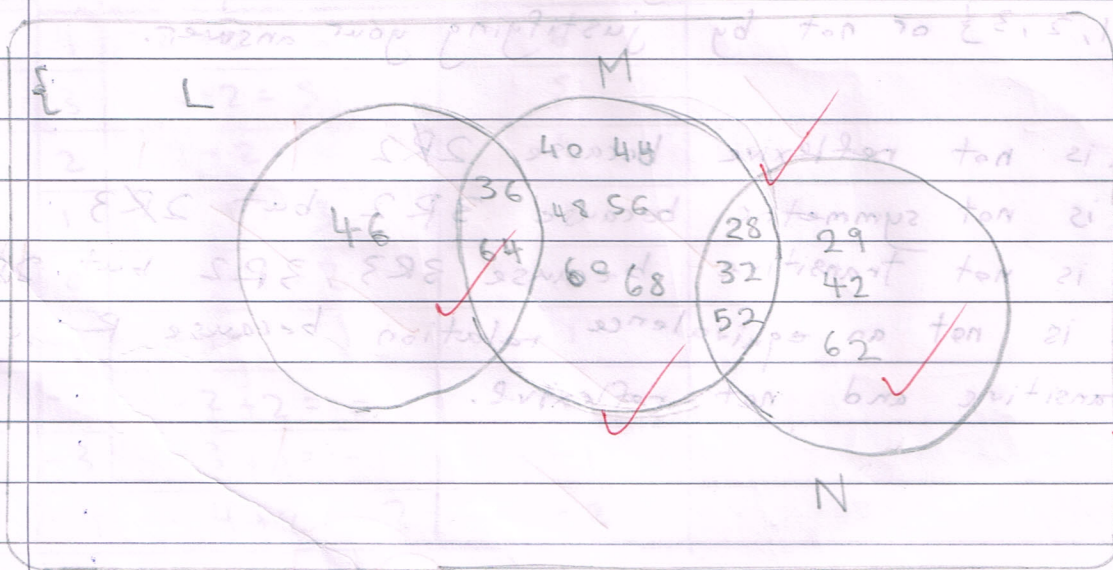
a) Sketch the venn diagram for the set $\{L, M \text{ and } N\}$.

a) $\{ = \{28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70\}$

- $L = \{36, 49, 64\}$

- $M = \{28, 32, 36, 40, 44, 48, 52, 56, 60, 64, 68\}$

- $N = \{28, 29, 32, 42, 52, 62\}$



Find all the elements of $n(M \cap N)$ and $n(L \cup M)$

b) $M \cap N = \{28, 32, 52\}$

$n(M \cap N) = 3$ ✓

$L \cup M = \{28, 32, 52, 40, 44, 48, 68, 56, 60, 64, 36, 49\}$

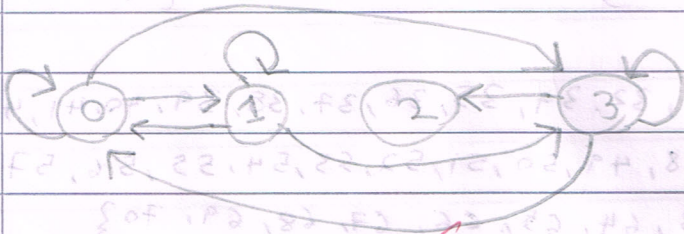
$n(L \cup M) = 12$ ✓

Question 2

Given $A = \{0, 1, 2, 3\}$ and the relation R on A is defined as follows:-

$R = \{(0, 0), (0, 1), (0, 3), (1, 0), (1, 1), (1, 3), (3, 0), (3, 2), (3, 3)\}$

a) Draw the directed graph of R relation



	in degree	out degree
0	3	3
1	2	3
2	1	0
3	3	3

b) Determine whether the given relation is equivalence on $\{0, 1, 2, 3\}$ or not by justifying your answer.

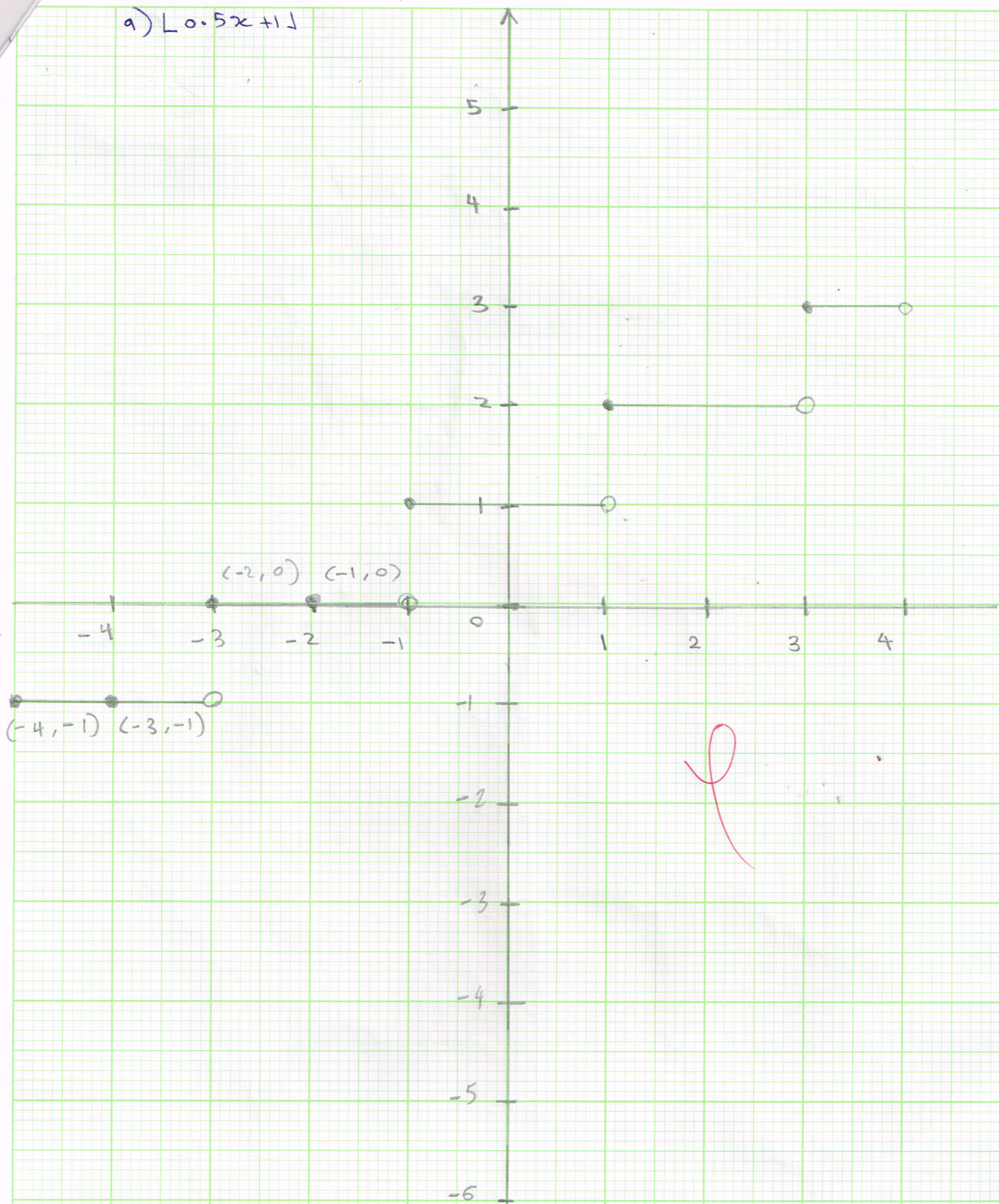
- R is not reflexive because $2 \not R 2$
- R is not symmetric because $3 R 2$ but $2 \not R 3$
- R is not transitive because $3 R 3, 3 R 2$ but $3 \not R 2$
- R is not an equivalence relation because R is not transitive and not reflexive.

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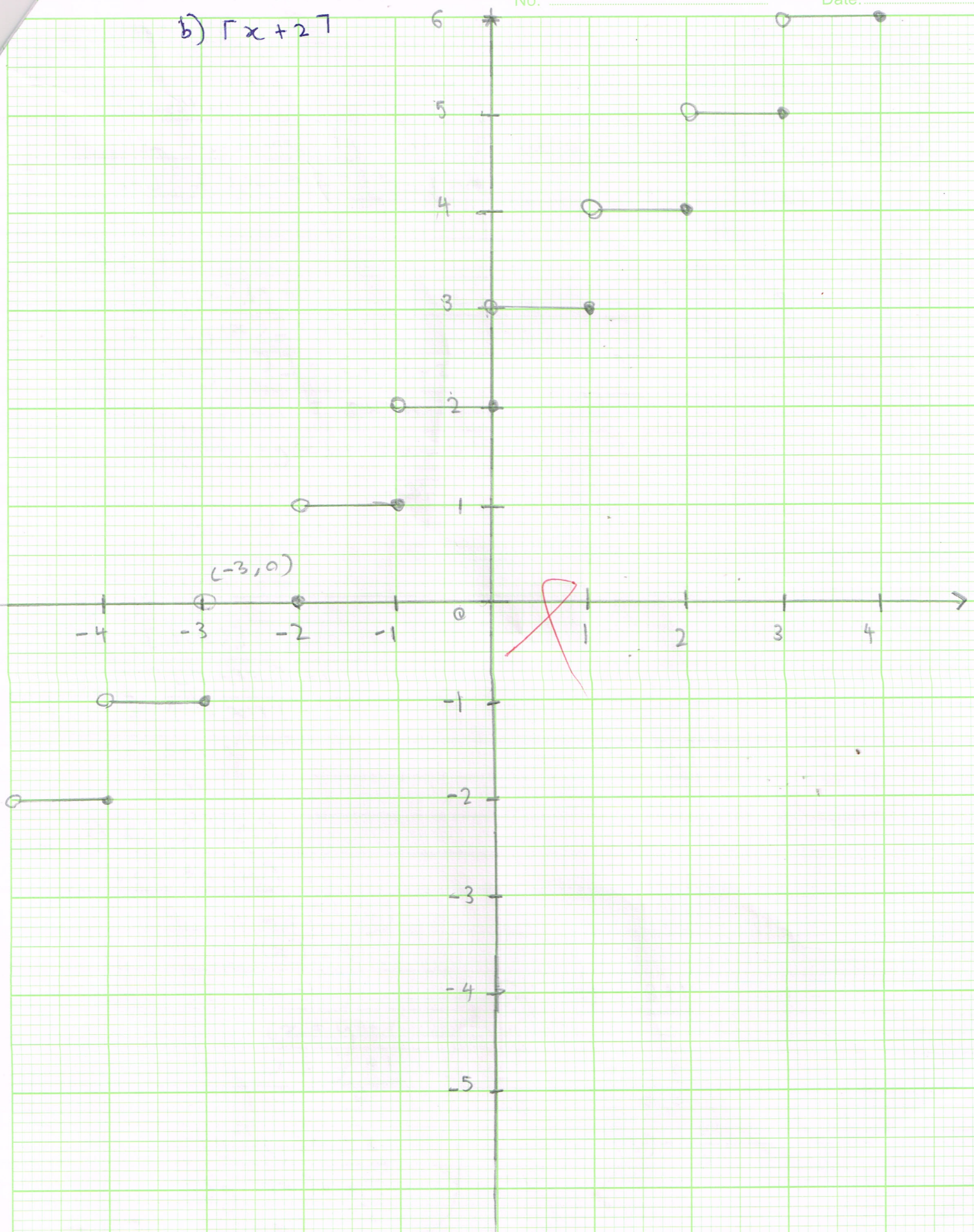
a) $L_{0.5x+1}$



No.

Date:

b) $\lceil x+2 \rceil$



Question 4

The functions f_g and F are given by $F_g: x \rightarrow 6x-1$ and $f: x \rightarrow 2-3x$. Find

a) g

$$F[g(x)] = 6x-1$$

$$2-3[g(x)] = 6x-1$$

$$-3[g(x)] = 6x-1-2$$

$$= 6x-3$$

$$g(x) = \frac{6x-3}{-3}$$

$$g(x) = 2x+1$$

b) gf

$$g[f(x)]$$

$$= 2[2-3x] + 1$$

$$= 4-6x+1$$

$$= 5-6x$$

c) $(fg)^{-1}(3)$

$$\text{Let } fg(x) = y$$

$$x = fg^{-1}(y)$$

$$fg(x) = y$$

$$6x-1 = y$$

$$6x = y+1$$

$$x = \frac{y+1}{6}$$

$$fg^{-1}(y) = \frac{y+1}{6}$$

$$fg^{-1}(x) = \frac{x+1}{6}$$

$$fg^{-1}(3) = \frac{3+1}{6}$$

$$= \frac{4}{6} = \frac{2}{3}$$

$$fg^{-1}(3) = \frac{2}{3}$$

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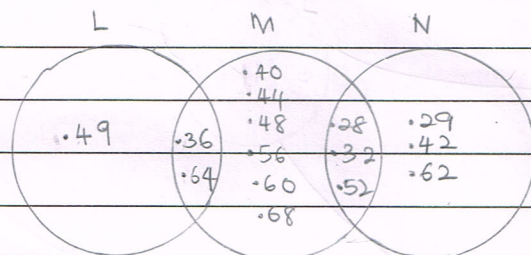
Date:.....

Question 1.

$$\text{Set } L = \{36, 49, 64\}$$

$$\text{Set } M = \{28, 32, 36, 40, 44, 48, 52, 56, 60, 64, 68\}$$

$$\text{Set } N = \{28, 29, 32, 42, 52, 62\}$$



• 30 • 41 • 54 • 67
 • 31 • 43 • 55 • 69
 • 33 • 45 • 57 • 70
 • 34 • 46 • 58
 • 35 • 47 • 59
 • 36 • 49 • 61
 • 37 • 50 • 63
 • 38 • 51 • 65
 • 39 • 53 • 66

b) $n(M \cap N)$

$$M \cap N = \{28, 32, 52\}$$

$$= 3$$

 $n(L \cup M)$

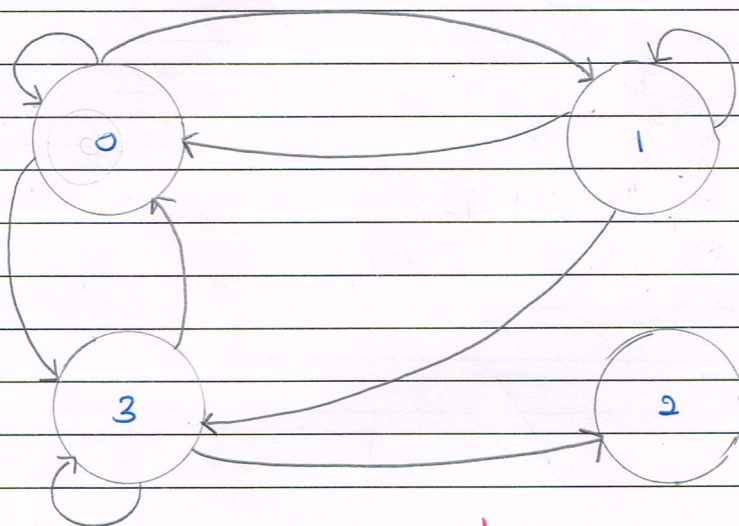
$$L \cup M = \{49, 36, 64, 40, 44, 48, 56, 60, 68\}$$

$$= 9$$

Question 2.

1. a) Diagram :

$$R = \{(0,0), (0,1), (0,3), (1,0), (1,1), (1,3), (3,0), (3,2), (3,3)\}$$



b) Reflexive :

- R is not reflexive because $2 \not R 2$.
- ~~R is reflexive because $0 R 0, 1 R 1$ and $2 R 3$~~

Symmetric :

- R is not symmetric because $3 R 2$ but $2 \not R 3$ and $1 R 3$ but $3 \not R 1$.
- ~~R is symmetric because $0 R 1$ and $1 R 0, 0 R 3$ and $3 R 0$.~~

Transitive :

- ~~R is transitive because whenever $0 R 1$, and $1 R 3$ then $0 R 3$ and whenever $1 R 0$ and $0 R 3$ then $1 R 3$~~
- ~~R is not transitive because $3 R 0$ and $0 R 1$ but $3 \not R 1$~~

$\therefore R$ is not equivalence because R is not reflexive, ~~not~~ symmetric and ~~not~~ transitive.

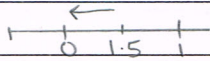
(3)

Question 3

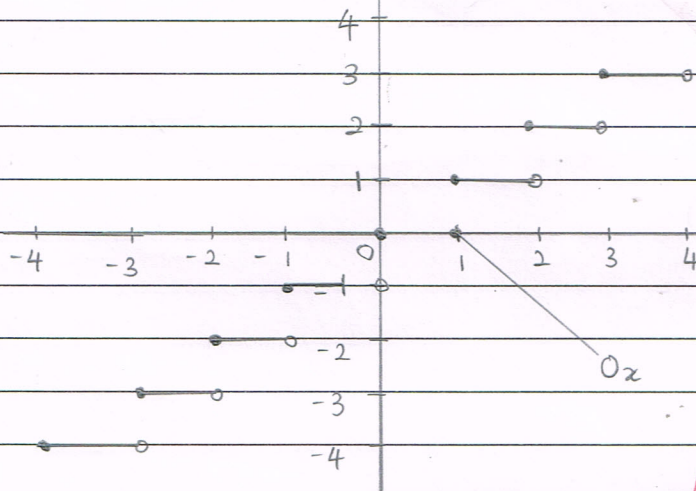
a) $\lfloor 0.5x + 1 \rfloor$

$0.5 + 1 = 1.5$

$\lfloor 1.5 \rfloor = 0$



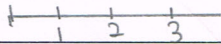
So, when x is 1.5, then $\lfloor 1.5 \rfloor = 0$



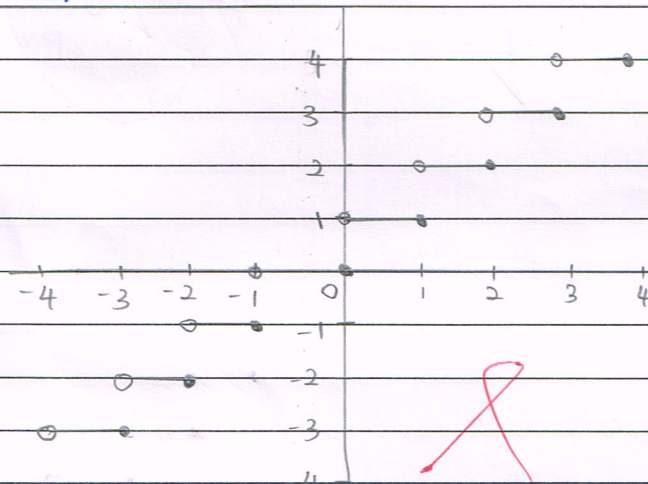
b) $\lceil x + 2 \rceil$

$x + 2 = 2$

$\lceil 2 \rceil = 2$



So, when $x = 2$, then $\lceil 2 \rceil = 2$



Question 4

The functions fg and f are given by $fg: x \rightarrow 6x-1$ and $f: x \rightarrow 2-3x$. Find x .

a) g

$$f(g(x)) = 6x-1$$

$$2-3(g(x)) = 6x-1$$

$$-3(g(x)) = 6x-1-2$$

$$= 6x-3$$

$$g(x) = \frac{6x-3}{-3}$$

$$g(x) = \frac{6x-3}{-3}$$

$$g(x) = -2x+1$$

b) gf

$$g(f(x))$$

$$= 2(2-3x)+1$$

$$= 4-6x+1$$

$$= 5-6x$$

c) $(fg)^{-1}(3)$

$$\text{Let } fg(x) = y$$

$$x = fg^{-1}(y)$$

$$fg(x) = y$$

$$6x-1 = y$$

$$6y = y+1$$

$$x = \frac{y+1}{6}$$

$$fg^{-1}(y) = \frac{y+1}{6}$$

$$fg^{-1}(x) = \frac{x+1}{6}$$

$$fg^{-1}(3) = \frac{3+1}{6}$$

$$= \frac{4}{6}$$

$$= \frac{2}{3}$$

$$fg^{-1}(3) = \frac{2}{3}$$