

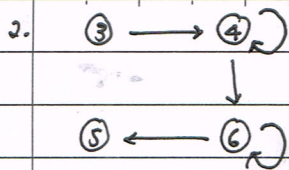
Revision Set 1

1. (a) $q \vee r \wedge \sim p$ $2^3 = 8$ rows

q	r	p	$\sim p$	$q \vee r$	$q \vee r \wedge \sim p$
T	T	T	F	T	F
T	T	F	T	T	T
T	F	T	F	T	F
T	F	F	T	T	T
F	T	T	F	T	F
F	T	F	T	T	T
F	F	T	F	F	F
F	F	F	T	F	F

(b) $(P \rightarrow q) \wedge (q \rightarrow r) \vee \sim r$ $2^3 = 8$ rows

P	q	r	$\sim r$	$(P \rightarrow q)$	$(q \rightarrow r)$	$(P \rightarrow q) \wedge (q \rightarrow r)$	$(P \rightarrow q) \wedge (q \rightarrow r) \vee \sim r$
T	T	T	F	T	T	T	T
T	T	F	T	T	F	F	T
T	F	T	F	F	T	F	F
T	F	F	T	F	T	F	T
F	T	T	F	T	T	T	T
F	T	F	T	T	F	F	T
F	F	T	F	T	T	T	T
F	F	F	T	T	T	T	T



$$R = \{(3,4), (4,4), (4,6), (6,6), (6,5)\}$$

Reflexive

R is not reflexive since $(3,3)$ and $(5,5) \notin R$.

Symmetric

R is not symmetric since $(3,4) \in R$ but $(4,3) \notin R$

Transitive

R is not transitive since $(4,6)$ and $(6,5) \in R$ but $(4,5) \notin R$

$\therefore R$ is not equivalence because R is not reflexive, not symmetric and not transitive.

3. $U = \{x \mid 20 \leq x \leq 30\}$

$$\{20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30\}$$

$$K = \{21, 27, 29\}$$

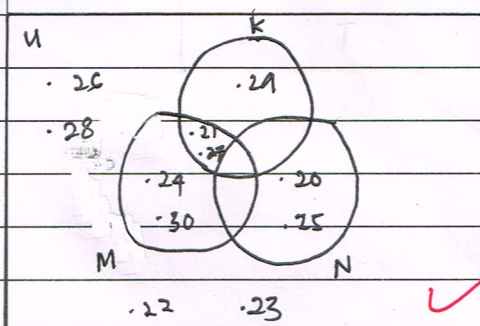
$$M = \{21, 24, 27, 30\}$$

$$N = \{20, 25\}$$

i) $(K \cup M') \cap N$

$$\{21, 27, 29, 26, 28, 22, 23, 20, 25\}$$

$$(K \cup M') \cap N = \{20, 25\}$$



iii) $(M - K)' \cap N$

$$M = \{21, 27, 24, 30\}$$

$$K = \{29, 21, 27\}$$

$$M - K = \{24, 30\}$$

$$(M - K)' = \{20, 21, 22, 23, 25, 26, 27, 28, 29\}$$

$$N = \{20, 25\}$$

$$(M - K)' \cap N = \{20, 21, 22, 23, 25, 26, 27, 28, 29\}$$

$$(M \cup K) - (N \cup K)$$

$$M \cup K = \{21, 24, 27, 29, 30\}$$

$$N \cup K = \{20, 21, 25, 27, 29\}$$

$$(M \cup K) - (N \cup K) = \{24, 30\}$$

4. P : He is rich

q : He is happy

(a) if he is rich, then he is unhappy.

$$P \rightarrow \sim q$$

(b) He is neither rich nor happy.

$$\sim P \wedge \sim q$$

(c) It is necessary to be poor in order to be happy.

$$q \rightarrow \sim p$$

(change sentence structure)

= If I am happy, then I am poor.

(d) He is unhappy if and only if he is poor.

$$\sim q \leftrightarrow \sim p$$

(e) To be poor is to be unhappy (if I am poor, then I am unhappy.)

$$\sim p \rightarrow \sim q$$