

 KEMENTERIA PENDIDIKAN MALAYSIA		 POLITEKNIK MALAYSIA		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS			
				COURSEWORK ASSESSMENT		QUIZ 3			
				SESSION		DECEMBER 2018			
				DURATION	15 MINS	CLO1	10 MARKS		
NAME		Mac Harry Anak Daren				CLO2			
REGISTRATION NO.		05DDT18F1662				CLO3			
PROGRAMME/ SECTION		DDT2A		TOTAL MARKS		10 MARKS			

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n+1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Question 1

$$a) 1 + 4 + 7 + 10 + \dots + (3n-2) = \frac{n(3n-1)}{2}$$

$P(n)$

$$P(1): (3(1)-2) = \frac{(1)(3(1)-1)}{2}$$

$$1 = \frac{2}{2}$$

$$1 = 1$$

Both sides are equal to 1.

b) $n = k$

$$1 + 4 + 7 + 10 + \dots + (3k-2) = \frac{k(3k-1)}{2}$$

$n = k+1$

$$\frac{k(3k-1)}{2} + (3(k+1)-2) = \frac{k(3k-1)}{2} + (3k+3-2)$$

$$\frac{k(3k-1)}{2} + (3k+1) = \frac{(k+1)(3(k+1)-1)}{2}$$

$$\begin{aligned} \frac{k(3k-1)}{2} + \frac{2(3k+1)}{2} &= \frac{(k+1)(3k+3-1)}{2} \\ \frac{k(3k-1) + 6k+2}{2} &= \frac{3k^2+2k+3k+2}{2} \\ 3k^2 - k + 6k + 2 &= 3k^2 + 2k + 3k + 2 \\ 3k^2 + 5k + 2 &= 3k^2 + 5k + 2 \end{aligned}$$

Question 2

$$f(1) : f(0+1) = \frac{2}{f(1)} + 3f(1)$$

$$f(1) = \frac{2}{1} + 3$$

$$f(1) = 5$$

$$f(2) : f(1+1) = \frac{2}{f(2)} + 3f(2)$$

$$f(2) = \frac{2}{2} + 6$$

$$= 7$$

$$f(3) : f(2+1) = \frac{2}{f(3)} + 3f(3)$$

$$f(3) = \frac{2}{3} + 9$$

$$= 9.67$$

$$f(4) : f(3+1) = \frac{2}{f(4)} + 3f(4)$$

$$f(4) = \frac{2}{4} + 12$$

$$= 12.5$$

 KEMENTERIA PENDIDIKAN MALAYSIA		 POLITEKNIK MALAYSIA		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
				COURSEWORK ASSESSMENT		QUIZ 3	
				SESSION		DECEMBER 2018	
				JABATAN MATEMATIK, SAINS DAN KOMPUTER		CLO1	10 MARKS
NAME	Ahmed Khalid bin Sutton			DURATION	15 MINS	CLO2	
REGISTRATION NO.	05DDT18F1119					CLO3	
PROGRAMME/ SECTION	DDT24					TOTAL MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

$$a) (3(1)-2) = \frac{1(3(1)-1)}{2}$$

$$3-2 = \frac{1(3-1)}{2}$$

$$1 = \frac{1(2)}{2}$$

$$1 = 1$$

both side is equal to 1

$$f(0) = 1$$

$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$

$$f(4+1) = \frac{2}{f(4)} + 3f(4)$$

$$\frac{2}{1/2} = 1/2$$

$$b) \frac{k+1}{2}$$

$$k+1 = \frac{k(3k-1)}{2}$$

$$3k-2 = \frac{k(3k-1)}{2}$$

Q2

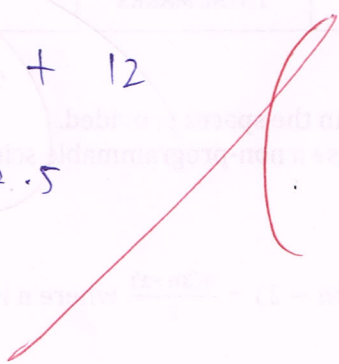
$$f(0)=1 \text{ and } f(n+1) = \frac{2}{f(n)} + 3f(n)$$

~~$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$~~

$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$

$$f(5) = \frac{1}{2} + 12$$

$$f(5) \approx 12.5$$



$$(1 - (1/2)^n) = 1 - (1/2)^n$$

$$(1 - 1/2) = 1/2$$

$$(1/2) = 1/2$$

both sides equal to 1/2

$$f(x) = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$$

$$f(x) = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$$

$$2k-2 = k(2k-1)$$

 KEMENTERIA PENDIDIKAN MALAYSIA		 POLITEKNIK MALAYSIA		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
				COURSEWORK ASSESSMENT		QUIZ 3	
				SESSION		DECEMBER 2018	
				DURATION	15 MINS	CLO1	10 MARKS
JABATAN MATEMATIK, SAINS DAN KOMPUTER							
NAME	Bonyface anak Jonathan						
REGISTRATION NO.	05DDT17F1031						
PROGRAMME/ SECTION	DDT4B			TOTAL MARKS		10 MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f_4(4)$.

Question 1) *Solusi*

$$a) 1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$$

$$\begin{aligned}
 &= 1 + 4 + 7 + \dots + (3n - 2) \\
 &= 1 + 4 + 7 + \dots + (3n - 2) + (3n - 2) \\
 &= \frac{n(3n-1)}{2} \\
 &= \frac{n(3n-1) + (3n-2)}{2} \\
 &= \frac{(3n^2 - 1) + (3n - 2)}{2} \\
 &= \frac{6n + 9}{2}
 \end{aligned}$$

b)

a) ~~Inductive step~~ ~~suppose~~

$$P(1) = \frac{(3 \cdot 1 - 2)}{2} = \frac{1(3 \cdot 1 - 1)}{2}$$

$$(3 \cdot 1 - 2) = 1 \frac{(3 \cdot 1 - 1)}{2}$$

$$1 = \frac{1(2)}{2}$$

$$1 = 1$$

~~P~~ ~~sa~~ $P(1)$ is true $1=1$

$$b) (3k - 2) = \frac{k(3k - 1)}{2}$$

$$(3k - 2) + (3(k+1) - 2) = \frac{k(3k - 1)}{2}$$

$$\frac{k(3k - 1)}{2} + 3(k+1) - 2 = \frac{(k+1)(3(k+1) - 1)}{2}$$

$$\frac{3k^2 - k + 6 + 2}{2} = \frac{3k^2 + 2k + 3k + 2}{2}$$

$$3k^2 + 5k + 2 = 3k^2 + 5k + 2$$

Q2 $f(0) = 1$ and $f(n+1) = \frac{2}{f(n)} + 3f(n)$

$$f(4)$$

$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$

$$= f(4+1) = \frac{2}{f(4)} + 3f(4)$$

$$\begin{aligned} f(5) &= \frac{2}{46.33} + 3 \cdot 46.33 \\ &= 0.043 + 138.99 \\ F(4) &= 139.033 \end{aligned}$$

$$f(3)$$

$$f(3+1) = \frac{2}{f(3)} + 3f(3)$$

$$f(3)$$

$\equiv$

 KEMENTERIA PENDIDIKAN MALAYSIA  POLITEKNIK MALAYSIA JABATAN MATEMATIK, SAINS DAN KOMPUTER		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
		COURSEWORK ASSESSMENT		QUIZ 3	
		SESSION		DECEMBER 2018	
		DURATION	15 MINS	CLO1	10 MARKS
				CLO2	
CLO3					
PROGRAMME/ SECTION		TOTAL MARKS		10 MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Question 1

$$\begin{aligned}
 b) & 1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2} \\
 & = 1 + 4 + 7 + 10 + \dots + (3k - 2) = \frac{k(3k-1)}{2} \\
 & \text{show } n = k+1 \\
 & = 1 + 4 + 7 + 10 + \dots + (3k - 2) + (3(k+1) - 2) = \frac{(k+1)(3(k+1)-1)}{2} \\
 & = \frac{k(3k-1)}{2} + (3k+3-2) = \frac{(k+1)(3k+3-1)}{2} \\
 & = \frac{k(3k-1)}{2} + 3k+1 = \frac{(k+1)(3k+2)}{2} \\
 & = k(3k-1) + 2(3k+1) = (k+1)(3k+2) \\
 & = 3k^2 - k + 6k + 2 = 3k^2 + 5k + 2 \\
 & = 3k^2 + 5k + 2 \text{ and } 3k^2 + 5k + 2
 \end{aligned}$$

a) $P(1)$

$$1 = (3(1) - 2) = \frac{1(3(1) - 1)}{2}$$

$$1 = (3 - 2) = \frac{1(3 - 1)}{2}$$

$$1 = 1 = \frac{1(2)}{2}$$

$$1 = 1 = \frac{2}{2}$$

$$1 = 1 = 1$$

= both sides equal to 1 ~~✗~~

2/2

Question 2

 KEMENTERIA PENDIDIKAN MALAYSIA  POLITEKNIK MALAYSIA JABATAN MATEMATIK, SAINS DAN KOMPUTER		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
		COURSEWORK ASSESSMENT		QUIZ 3	
		SESSION		DECEMBER 2018	
		DURATION	15 MINS	CLO1	10 MARKS
NAME	Syahirah binti Yaman			CLO2	
REGISTRATION NO.	0900718F1073			CLO3	
PROGRAMME/ SECTION	DDT 2A - S1	TOTAL MARKS		10 MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Q1(a)

$$1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$$

If $P(1)$ is true, then ...

$$(3(1) - 2) = 1(3(1) - 1)$$

$$1 = \frac{1(3-1)}{2}$$

$$1 = \frac{1(2)^2}{2}$$

$$1 = 1$$

$P(1)$ is true because both are equal to 1.

3

(b) Inductive step:

$$\text{change } 1+4+7+10+\dots+(3n-2) = \frac{n(3n-1)}{2}$$

$$\text{to } 1+4+7+10+\dots+(3n-2) = \frac{n + (3n-1)}{2}$$

$$(\cancel{3k+1}-2) \Rightarrow$$

$$(3k-2) = k + \frac{(3k-1)}{2}$$

Q2

$$f(0)=1, f(n+1) = \frac{2}{f(n)} + 3f(n) \quad \text{count } f(4).$$

$$f(0+1) = \frac{2}{f(0)} + 3f(0)$$

$$\cancel{f(1)} = \frac{2}{\cancel{f(0)}} \quad f(1) = \frac{2}{1} + 3(1)$$

$$f(1) = 2 + 3(1)$$

$$f(1) = 2 + 3$$

$$f(1) = 5$$

$$f(1) = 5,$$

$$f(5+1) = \frac{2}{f(5)} + 3f(5)$$

$$f(6) = \frac{2}{f(5)} + 3f(5)$$

$$\underline{f(5-1) = 2}$$

$$\cancel{f(4+1)} = \frac{2}{\cancel{f(4)}} +$$

$$f(0+4+1) = \frac{2}{f(0+4)} + 3f(0+4)$$

$$f(5) = \frac{2}{f(4)} + 3f(4)$$

$$f(3+1) = \frac{2}{f(3)} + 3f(3)$$

$$f(4) = \frac{2}{f(3)} + 3f(3)$$

 KEMENTERIA PENDIDIKAN MALAYSIA		 POLITEKNIK MALAYSIA		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
				COURSEWORK ASSESSMENT		QUIZ 3	
				SESSION		DECEMBER 2018	
				JABATAN MATEMATIK, SAINS DAN KOMPUTER		CLO1	10 MARKS
NAME	ASMA ARIYAH BT. BERANI	DURATION	15 MINS	CLO2			
REGISTRATION NO.	0500718 F1046			CLO3			
PROGRAMME/ SECTION	DDT2A			TOTAL MARKS		10 MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n+1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Q1:

$$a) P(1) = (3(1) - 2) = \frac{1(3(1) - 1)}{2}$$

$$1 = (3(1) - 2) = \frac{1(3(1) - 1)}{2}$$

$$1 - 1 = 0 = \frac{2}{2} = 1$$

because

$P(1)$ is true Both sides equal to 1

$$b) 3k = 1 + 4 + 7 + 10 + \dots +$$

$$3k - 2 = \frac{k(3k - 1)}{2}$$

$$\frac{3k - 2}{2} = \frac{k^2(3k^2 - 1)}{2}$$

$$\frac{3(1) - 2}{2} = \frac{(1)^2(3(1)^2 - 1)}{2}$$

Question 2

$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$

$$f(1+1) = \frac{2}{f(1)} + 3f(1) = \frac{2}{1} + 3(1) = 5$$

$$f(1+2) = \frac{2}{f(2)} + 3f(2) = \frac{2}{2} + 3(2) = 10$$

$$f(1+3) = \frac{2}{f(3)} + 3f(3) = \frac{2}{3} + 3(3) = 15$$

$$f(1+4) = \frac{2}{f(4)} + 3f(4) = \frac{2}{4} + 3(4) = 20$$

1

0

$$\frac{(1 - (1/2)^n) - 1}{1 - (1/2)^n} = \frac{(1/2)^n - 1}{1 - (1/2)^n} = -1$$

$$\frac{1 - (1/2)^n}{1 - (1/2)^n} = 1$$

3

for large n, 2^n is equal to 1

$$2^n = 1 + 10 + 10 + \dots$$

$$2^n - 1 = 10 + 10 + \dots$$

$$2^n - 1 = 10 + 10 + \dots$$

$$\frac{2^n - 1}{2} = \frac{10 + 10 + \dots}{2}$$

 KEMENTERIA PENDIDIKAN MALAYSIA				COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
				COURSEWORK ASSESSMENT		QUIZ 3	
				SESSION		DECEMBER 2018	
				JABATAN MATEMATIK, SAINS DAN KOMPUTER		DURATION	
CLO2							
CLO3							
NAME		Muhamad Audi Bin Pasha		TOTAL MARKS		10 MARKS	
REGISTRATION NO.		05DDT18F1099					
PROGRAMME/ SECTION		DD2A					

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
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Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Question 1

(a) $P(1) \quad 3(1) - 2 = \frac{1(3(1)-1)}{2}$

$3 - 2 = \frac{1(3-1)}{2}$

$1 = 1 \quad (\text{TRUE})$

(b) $1 + 4 + 7 + 10 + \dots + (3k-2) = \frac{k(3k-1)}{2}$

INDUCTIVE STEP

$1 + 4 + 7 + 10 + \dots + (3k-2) + (3(k+1)-2) = \frac{(k+1)(3(k+1)-1)}{2}$

$\frac{k(3k-1)}{2} + (3k+3-2) = \frac{(k+1)(3k+3-1)}{2}$

$k(3k-1) + 2(3k+1) = (k+1)(3k+2)$

$3k^2 - k + 6k + 2 = 3k^2 + 2k + 3k + 2$

$3k^2 + 5k + 2 = 3k^2 + 5k + 2 \quad \#$

Question 2

$$f(0) = 1$$

$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$

$$f(1) = f(0+1) = \frac{2}{f(0)} + 3f(0)$$

$$= \frac{2}{1} + 3(1)$$

$$= 2 + 3$$

$$= 5$$

$$f(2) = f(1+1) = \frac{2}{f(1)} + 3f(1)$$

$$= \frac{2}{5} + 3(5)$$

$$= \frac{2}{5} + 15$$

$$= 15.4$$

$$f(3) = f(2+1) = \frac{2}{f(2)} + 3f(2)$$

$$= \frac{2}{15.4} + 3(15.4)$$

$$= 46 \frac{127}{385}$$

$$= 46.33$$

$$f(4) = f(3+1) = \frac{2}{f(3)} + 3f(3)$$

$$= \frac{2}{46.33} + 3(46.33)$$

$$= \frac{2}{46.33} + 138.99$$

$$= 139.033$$

 KEMENTERIA PENDIDIKAN MALAYSIA  POLITEKNIK MALAYSIA JABATAN MATEMATIK, SAINS DAN KOMPUTER		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS			
		COURSEWORK ASSESSMENT		QUIZ 3			
		SESSION		DECEMBER 2018			
		DURATION	15 MINS	CLO1	10 MARKS		
CLO2							
CLO3							
NAME		Freedy Fooster ak Basi					
REGISTRATION NO.		05DDTBF1125					
PROGRAMME/ SECTION		DDT2A		TOTAL MARKS		10 MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Answer

Question 1 (a)

$$P(n) = P(1) = 1 + 4 + 7 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$$

Insert (1) in n;

$$(3(1) - 2) = \frac{1(3(1) - 1)}{2}$$

$$3 - 2 = \frac{3 - 1}{2}$$

$$1 = \frac{2}{2}$$

$$1 = 1$$

∴ Both side equals to 1

Question 1 (b)

$$\frac{k(3k+1)}{2} + 3(k+1) - 2 = \frac{(k+1)(3k+1)}{2} - 1$$

$$\frac{3k^2 - 3k}{2} + 3(k+1) - 2 = \frac{(k+1)(3k+3-1)}{2}$$

$$\frac{3k^2 - k}{2} + 3k + 3 - 2 = \frac{3k^2 + 3k - k + 3k + 3 - 1}{2}$$

$$\frac{3k^2 + 2k + 1}{2} = \frac{3k^2 + 5k + 2}{2}$$

3

Question 2.

Info:

$$f(0) = 1$$

$$f(n+1) = \frac{2}{f(n)} + 3f(n)$$

Answer

(1)

$$f(1) = \frac{2}{f(1-1)} + 3f(1-1)$$

$$f(1) = \frac{2}{f(0)} + 3f(0)$$

$$f(1) = \frac{2}{1} + 3(1)$$

$$f(1) = 2 + 3$$

$$f(1) = 5$$

$$f(2) = \frac{2}{f(2-1)} + 3f(2-1)$$

$$f(2) = \frac{2}{f(1)} + 3f(1)$$

$$f(2) = \frac{2}{5} + 3(5)$$

$$f(2) = \frac{2}{5} + 15$$

$$f(2) = 15.4$$

$$f(3) = \frac{2}{f(3-1)} + 3f(3-1)$$

$$f(3) = \frac{2}{f(2)} + 3f(2)$$

$$f(3) = \frac{2}{15.4} + 3(15.4)$$

$$f(3) = \frac{2}{15.4} + 46.2$$

$$f(3) = 46.33$$

$$f(4) = \frac{2}{f(4-1)} + 3f(4-1)$$

$$f(4) = \frac{2}{f(3)} + 3f(3)$$

$$f(4) = \frac{2}{46.33} + 3(46.33)$$

$$f(4) = \frac{2}{46.33} + 138.99$$

$$f(4) = 139.04$$

 KEMENTERIA PENDIDIKAN MALAYSIA		 POLITEKNIK MALAYSIA		COURSE CODE/ COURSE NAME		DBM2033 DISCRETE MATHEMATICS	
				COURSEWORK ASSESSMENT		QUIZ 3	
				SESSION		DECEMBER 2018	
				JABATAN MATEMATIK, SAINS DAN KOMPUTER			
NAME	Frederick Jack			DURATION	15 MINS	CLO1	10 MARKS
REGISTRATION NO.	05DDT18F1112					CLO2	
PROGRAMME/ SECTION	DDT2A					CLO3	
				TOTAL MARKS		10 MARKS	

Instructions

- Answer ALL questions. Write your answers in the spaces provided.
- Show your working to get marks. You may use a non-programmable scientific calculator.

Question 1

CLO2, C3

[6 marks]

Let $P(n)$ is the statement of $1 + 4 + 7 + 10 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$, where n is all positive integer.

- Show that $P(1)$ is true.
- Complete the inductive step.

Question 2

CLO2, C2

[4 marks]

Suppose f is recursively defined by $f(0) = 1$ and $f(n + 1) = \frac{2}{f(n)} + 3f(n)$.

Count $f(4)$.

Question 1

$$a) P(1) : (3(1) - 2) = \frac{1(3(1) - 1)}{2}$$

$$1 = (3 - 2) = \frac{1(2)}{2}$$

$$1 = 1 = \frac{2}{2}$$

$$1 = 1 = 1$$

$$b) (3k - 2) = k(3k - 1)$$

$$(3k - 2) + (3(k+1) - 2) = \frac{k(3k - 1)}{2}$$

$$\frac{k(3k - 1)}{2} + (3(k+1) - 2) = \frac{(k+1)(3(k+1) - 1)}{2}$$

$$\frac{3k^2 - k}{2} + \frac{2(3k+1)}{2} = \frac{(k+1)(3k+2)}{2}$$

$$\frac{3k^2 - k + 6k + 2}{2} = \frac{3k^2 + 5k + 2}{2}$$

$$3k^2 + 5k + 2 = 3k^2 + 5k + 2$$

Question 2

$$f(1) = \frac{2}{f(1-1)} + 3f(1-1)$$

$$\frac{2}{f(0)} + 3f(0)$$

$$\frac{2}{1} + 3(1)$$

$$2 + 3$$

$$= 5$$

$$f(1+1) = \frac{2}{f(2-1)} + 3f(2-1)$$

$$f(2) = \frac{2}{f(1)} + 3f(1)$$

$$= \frac{2}{5} + 3(5)$$

$$= 0.4 + 15$$

$$= 15.4$$

$$f(2+1) = \frac{2}{f(3-1)} + 3f(3-1)$$

$$f(3) = \frac{2}{f(2)} + 3f(2)$$

$$= \frac{2}{f(15.4)} + 3f(15.4)$$

$$= \frac{2}{15.4} + 46.2$$

$$= 0.13 + 46.2$$

$$= 46.33$$

$$f(3+1) = \frac{2}{f(4-1)} + 3f(4-1)$$

$$f(4) = \frac{2}{f(3)} + 3f(3)$$

$$= \frac{2}{f(46.33)} + 3f(46.33)$$

$$= \frac{2}{46.33} + 138.99$$

$$= 0.043 + 138.99$$

$$= 139.033$$

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