

Self-Exercise 16

Differentiate the function with respect to x

①

$$y = 3x^4$$
$$\frac{dy}{dx} = 3(4)x^{4-1}$$
$$= 12x^3$$

②

$$y = 7x^3$$
$$\frac{dy}{dx} = 7(3)x^{3-1}$$
$$= 21x^2$$

③

$$y = 14x^2$$
$$\frac{dy}{dx} = 14(2)x^{2-1}$$
$$= 28x$$

④

$$y = x^4$$
$$\frac{dy}{dx} = 1(4)x^{4-1}$$
$$= 4x^3$$

⑤

$$y = \frac{1}{x^2}$$
$$\frac{dy}{dx} = 1(-2)x^{-2-1}$$
$$= -2x^{-3}$$
$$= -2\left(\frac{1}{x^3}\right)$$
$$= \frac{-2}{x^3}$$

⑥

$$y = \frac{7}{x}$$
$$\frac{dy}{dx} = 7(-1)x^{-1-1}$$
$$= -7x^{-2}$$
$$= -7\left(\frac{1}{x^2}\right)$$
$$= \frac{-7}{x^2}$$

⑦

$$y = 6x^{-6}$$
$$\frac{dy}{dx} = 6(-6)x^{-6-1}$$
$$= -36x^{-7}$$
$$= -36\left(\frac{1}{x^7}\right)$$
$$= \frac{-36}{x^7}$$

⑧

$$y = \frac{1}{4}x^6$$
$$\frac{dy}{dx} = \frac{1}{4}(6)x^{6-1}$$
$$= \frac{3}{2}x^5$$

$$\begin{aligned} \textcircled{9} \quad y &= x^2 + x^3 \\ \frac{dy}{dx} &= 1(2)x^{2-1} + 1(3)x^{3-1} \\ &= 2x + 3x^2 \end{aligned}$$

$$\begin{aligned} \textcircled{10} \quad y &= 5x - 10x^2 \\ \frac{dy}{dx} &= 5(1)x^{1-1} - 10(2)x^{2-1} \\ &= 5 - 20x \end{aligned}$$

$$\begin{aligned} \textcircled{11} \quad y &= x^2 - 3x^4 \\ \frac{dy}{dx} &= 1(2)x^{2-1} - 3(4)x^{4-1} \\ &= 2x - 12x^3 \end{aligned}$$

$$\begin{aligned} \textcircled{12} \quad y &= 9 + 4x^2 \\ \frac{dy}{dx} &= 0 + 4(2)x^{2-1} \\ &= 8x \end{aligned}$$

$$\begin{aligned} \textcircled{13} \quad y &= 3x + \frac{1}{4}x^2 \\ \frac{dy}{dx} &= 3(1)x^{1-1} + \frac{1}{4}(2)x^{2-1} \\ &= 3x^0 + \frac{1}{2}x \end{aligned}$$

$$\begin{aligned} \textcircled{14} \quad y &= 2x^{-1} - x^{-2} \\ \frac{dy}{dx} &= 2(-1)x^{-1-1} - 1(-2)x^{-2-1} \\ &= -2x^{-2} + 2x^{-3} \\ &= -2\left(\frac{1}{x^2}\right) + 2\left(\frac{1}{x^3}\right) \\ &= \frac{-2}{x^2} + \frac{2}{x^3} \end{aligned}$$

$$\begin{aligned} \textcircled{15} \quad y &= 4x^{\frac{1}{2}} + \frac{1}{4}x^2 \\ \frac{dy}{dx} &= 4\left(\frac{1}{2}\right)x^{\frac{1}{2}-1} + \frac{1}{4}(2)x^{2-1} \\ &= 2x^{-\frac{1}{2}} + \frac{1}{2}x \\ &= 2\left(\frac{1}{x^{\frac{1}{2}}}\right) + \frac{1}{2}x \\ &= \frac{2}{\sqrt{x}} + \frac{1}{2}x \end{aligned}$$