

worksheet 1

1 a) $2+7=10$ ~~False.~~

This is ~~unknown~~ proposition.

$x+7=10.$

~~This is not proposition.~~
~~because it is an unknown.~~

b) $4+7 > 11$

This is ~~proposition~~ and truth values is false

c) A triangle is a four-sided polygon

This is proposition ~~and~~ the truth values is ~~false~~ because triangle only have three-sided polygon.

d) This sentence is false.

This is proposition ~~and~~ the truth values ~~Command~~ ?
~~Not proposition.~~

e) Tea comes with dinner.

This is proposition and the truth values ~~is True.~~
~~either true or false.~~f) What is your auntie's name? ~~Not proposition.~~

It is a question.

2 a) Proposition

- A proposition is typically expressed as a declarative sentence which is either true or false but not both.

b) Compound Statement

- Statements or propositional variables can be combined by logical connectives to obtain compound statements.

3. a) P and R

- A week has seven days and there are 60 minutes in an hour. The truth values is true.

b) $P \wedge Q$

- A week has seven days and there are 20 hours in a day. The truth values is false because there are 24 hours only in a day.

c) $R \vee Q$

- There are 60 minutes in an hour or there are 20 hours in a day. The truth values is true because there are 60 minutes in an hour.

d) $Q \vee P$

- There are 20 hours in a day or there are 60 minutes in an hour. A week has seven days. The truth values is true because there are seven days in a week.

4. B Truth table based on question 3

(b)

(d)

~~car~~~~for~~

for two variables

P	Q	$P \wedge Q$	$Q \vee P$
T	T	T	T
T	F	F	T
F	T	F	T
F	F	F	F

~~P and R~~

3 variables

P	Q	R	$P \wedge R$	$R \vee Q$	$P \wedge Q$	$Q \vee P$
T	T	T	T	T	T	T
T	T	F	F	T	T	T
T	F	T	T	T	F	T
T	F	F	F	F	F	T

Negation and truth table

There exists a classroom in which no chair is broken.

5. a) All classrooms have at least one chair that is broken.

- It is not the case that all classrooms have at least one chair that is broken. ✓

b) No classroom has only chairs that are broken.

- It is not the case ^{that} no classrooms has only chairs that are broken. ✓

There exists a classroom that has only chairs that are not broken.

c) Every student in this class has taken discrete mathematics or computing mathematics.

- It is not the case that every student in their this class has taken discrete mathematics or computing mathematics. ✓

There exists a student in this class who has neither taken discrete mathematics nor computing mathematics.

6. a) $\neg q \rightarrow (\neg p \vee q)$

p	q	$\neg p$	$\neg q$	$(\neg p \vee q)$	$\neg q \rightarrow (\neg p \vee q)$
T ✓	F	F ✓	F	T F ✓	F ✓ T
T ✓	F	F ✓	T	F ✓	F ✓
F ✓	T	T ✓	F	T ✓	T ✓
F ✓	F	T ✓	T	T ✓	T ✓

b) $(p \wedge q) \vee \sim p$

p	q	$p \wedge q$	$\sim p$	$(p \wedge q) \vee \sim p$
T ✓	T ✓	T ✓	F ✓	T ✓
T ✓	F ✓	F ✓	F ✓	F ✓
F ✓	T ✓	F ✓	T ✓	T ✓
F ✓	F ✓	F ✓	T ✓	T ✓

c) $(\sim p \rightarrow q) \vee (\sim p \wedge \sim q)$

p	q	$\sim p$	$\sim q$	$(\sim p \rightarrow q)$	$(\sim p \wedge \sim q)$
T ✓	T ✓	F ✓	F ✓	F T ✓	F ✓ ✓
T ✓	F ✓	F ✓	T ✓	T ✓	F ✓ ✓
F ✓	T ✓	T ✓	F ✓	T ✓	F ✓ ✓
F ✓	F ✓	T ✓	T ✓	T F ✓	T ✓ ✓

$(\sim p \rightarrow q) \vee (\sim p \wedge \sim q)$

F	✗	T
T	✓	
T	✓	
T	✓	

$A \rightarrow B$
condition consequences.