

Final Exam

Date

No.

Question 5

$$\begin{aligned}
 \text{a) i)} \quad & \frac{6^2 x^6}{6^5} \\
 & = \frac{6^2 \cancel{6^3} x^6}{\cancel{6^3}} = 6^{2-5} x^6 \\
 & = 6^{-3} x^6 \\
 & = \frac{1}{6^3} x^6 \\
 & = \frac{x^6}{216} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{ii)} \quad & (2^n \times 8^{2n})^{\frac{1}{n}} \\
 & = (2^n \times (2^3)^{2n})^{\frac{1}{n}} \\
 & = (2^n \times 2^{6n})^{\frac{1}{n}} \\
 & = (2^{7n})^{\frac{1}{n}} \\
 & = 2^7 \\
 & = 128 \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{b) i)} \quad & 4^{2x+1} \\
 & = \frac{4^{3+x} \times 4^{2x}}{4^{2x+5}} \checkmark \\
 & = \frac{1}{4^{2x+5-(2x+1)}} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 & = \frac{1}{4^{2x+5-2x-1}} \checkmark \\
 & = \frac{1}{4^{4}} \checkmark \\
 & = \frac{1}{256} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 & 2x+1 - (2x+5) \\
 & = 2x+1-2x-5 \\
 & = -4 \\
 & = \frac{1}{4^4}
 \end{aligned}$$

$$\begin{aligned}
 \text{ii)} \quad & \frac{7^{2(k+3)} \times 7^{3k+2} \times 7^{2-k}}{49^{5+3k}} \checkmark \\
 & = \frac{7^{2k+6} \times 7^{3k+2} \times 7^{2-k}}{(7^2)^{5+3k}} \checkmark \\
 & = \frac{7^{2k+6+3k+2+2-k}}{7^{10+6k}} \checkmark \\
 & = \frac{7^{4k+10}}{7^{10+6k}} \checkmark \\
 & = 7^{4k+10-10-6k} \checkmark \\
 & = 7^{4k-6k} \checkmark \\
 & = 7^{-2k} \checkmark \\
 & = \frac{1}{7^{2k}} \checkmark \\
 & = \frac{1}{49^k} \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{c) i)} \quad 27^{2x+10} &= 9^{3x} (3^{5x}) \\
 (3^3)^{2x+10} &= (3^2)^{3x} \times 3^{5x} \\
 3^{6x+30} &= 3^{6x} \times 3^{5x} \\
 3^{6x+30} &= 3^{11x} \\
 6x+30 &= 11x \\
 6x+30-30 &= 11x-30 \\
 6x-11x &= 11x-11x-30 \\
 -5x &= -30 \\
 \frac{-5}{-5} \quad \frac{-30}{-5} \\
 x &= 6
 \end{aligned}$$

$$\begin{aligned}
 \text{ii)} \quad 8^{3k} - 64^{5-k} &= 0 \\
 8^{3k} - (8^2)^{5-k} &= 0 \\
 8^{3k} - 8^{10-2k} &= 0 \\
 3k - (10-2k) &= 0 \\
 3k - 10 + 2k &= 0 \\
 3k - 10 + 10 + 2k &= 10 \\
 \frac{5k}{5} &= \frac{10}{5} \\
 k &= 2
 \end{aligned}$$

Checked.
29/9/18.