

Revision Set 2

$$f(x) = 2x - 1$$

$$g(x) = 3x$$

$$h(x) = x^2 + 1$$

$$(a) f(x+1) = 2(x+1) - 1$$

$$= 2x + 2 - 1$$

$$= 2x + 1$$

$$(b) (g \circ h)(24)$$

$$(g \circ h)(x) = g[h(x)]$$

$$= g(x^2 + 1)$$

$$= 3(x^2 + 1)$$

$$(g \circ h)(24) = 3x^2 + 3$$

$$= 3(24)^2 + 3$$

$$= 1731$$

$$(c) g(3a) = 3(3a)$$

$$= 9a$$

$$2. a) f(x) = \frac{-3}{x-3}$$

$$\text{let } y = \frac{-3}{x-3}$$

$$y(x-3) = -3$$

$$xy - 3y = -3$$

$$xy = -3 + 3y$$

$$\frac{xy}{y} = \frac{-3 + 3y}{y}$$

$$x = \frac{-3 + 3y}{y}$$

$$f(x)^{-1} = \frac{-3 + 3x}{x}, x \neq 0$$

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$$2. b) g(x) = \frac{12 - 3x}{4}$$

$$\text{let } y = \frac{12 - 3x}{4}$$

$$4y = 12 - 3x$$

$$3x = 12 - 4y$$

$$\frac{3x}{3} = \frac{12 - 4y}{3}$$

$$x = \frac{12 - 4y}{3}$$

$$g(x)^{-1} = \frac{12 - 4y}{3}$$

$$3. a) \lfloor -3.4 \rfloor \times \lceil 2.8 \rceil$$

$$= -4 \times 3$$

$$= -12$$

$$b) \lfloor -0.82 \rfloor \times 0.3$$

$$= \lceil -1 \times 0.3 \rceil$$

$$= \lceil -0.3 \rceil$$

$$= 0$$

$$\lceil \lfloor -2.2 \times 0.3 \rfloor + (-1.78) \rceil$$

$$= \lceil \lfloor -0.66 \rfloor + (-1.78) \rceil$$

$$= \lceil -1 + (-1.78) \rceil$$

$$= \lceil -2.78 \rceil$$

$$= -2$$

$$P: \{11, 12, 13, 14, 15\}$$

$$Q: \{10, 12, 14, 16, 18\}$$

$$R: \{7, 9, 11, 14, 18, 20\}$$

$$(a) Q - R = \{10, 12, 16\}$$

In Q not in R ✓

$$(b) R - P = \{7, 9, 18, 20\}$$

$$5. \{0, 1, 2\}$$

$$(a) \{(0,0), (1,1), (2,2)\}$$

Reflexive

- all the elements loop to itself ✓

Symmetric

- all the elements whenever aRb , then bRa ✓

Transitive

- all the elements whenever aRb , bRa then aRc . ✓

∴ R is equivalence relation since it is reflexive, symmetric and transitive. ✓

$$(b) \{(0,0), (1,1), (2,2), (0,1), (1,2)\}$$

Reflexive

- all element loop to itself since $(0,0), (1,1), (2,2)$. ✓

Symmetric

- R is not symmetric since $(0,1)$ in the relation but $(1,0)$ not in the relation. ✓

Transitive

- R is not Transitive since $(0,1)$ and $(1,2)$ in R but $(0,2)$ not in R. $0R1, 1R2$ but $0R2$ ✓

∴ R is not equivalence relation since R is reflexive but not symmetric and not transitive. ✓