

Self Exercise 9

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~~1 a) $x + 9$~~

Solve the following equations. $2 + m (2)$

1 a) $x + 9 = 20$

$x + 9 - 9 = 20 - 9$

$x = 11$

b) $x - 8 = 10$

$x - 8 + 8 = 10 + 8$

$x = 18$

c) $x + 1.6 = 2.4$

$x + 1.6 - 1.6 = 2.4 - 1.6$

$x = 0.8$

d) $y - 2 = -8$

$y - 2 + 2 = -8 + 2$

$y = -6$

e) $x - \frac{3}{4} = 1\frac{1}{2}$

$x - \frac{3}{4} + \frac{3}{4} = 1\frac{1}{2} + \frac{3}{4}$

$x = \frac{3}{2} + \frac{3}{4}$

$x = \frac{6}{4} + \frac{3}{4}$

$x = \frac{9}{4}$

$x = 1\frac{1}{4}$

$x = 1\frac{1}{4}$

$2 \overline{) 2, 4}$

$2 \overline{) 1, 2}$

$1, 2$

$2 \overline{) 9}$

8

1

$x = 2\frac{1}{4}$

$$f) m + 6 = -4$$

$$m + 6 - 6 = -4 - 6$$

$$m = -10$$

$$g) m - 7 \cdot 1 = -8 \cdot 4$$

$$m - 7 \cdot 1 + 7 \cdot 1 = -8 \cdot 4 + 7 \cdot 1$$

$$m = -1 \cdot 3$$

$$h) x + \frac{1}{2} = 2$$

$$x + \frac{3}{2} = 2$$

$$x + \frac{3}{2} - \frac{3}{2} = 2 - \frac{3}{2}$$

$$x = 2 - \frac{3}{2}$$

$$= \frac{4}{2} - \frac{3}{2}$$

$$= \frac{1}{2}$$

$$i) y + 80 = 120$$

$$y + 80 - 80 = 120 - 80$$

$$y = 40$$

Solve the following equations

a) $2x = 11$

$$\frac{2x}{2} = \frac{11}{2}$$

$$x = \frac{11}{2}$$

e) $\frac{x}{3} = 1.2$

$$\frac{x}{3} \times 3 = 1.2 \times 3$$

$$x = 3(1.2)$$

$$x = 3.6$$

b) $4x = 20$

$$\frac{4x}{4} = \frac{20}{4}$$

$$x = \frac{20}{4}$$

$$x = 5$$

f) $\frac{x}{5} = 5$

$$\frac{x}{5} \times 5 = 5 \times 5$$

$$x = 5(5)$$

$$x = 25$$

c) $3x = -24$

$$\frac{3x}{3} = \frac{-24}{3}$$

$$x = \frac{-24}{3}$$

$$x = -8$$

g) $\frac{x}{2} = -7$

$$\frac{x}{2} \times 2 = -7 \times 2$$

$$x = -7(2)$$

$$x = -14$$

d) $6x = 24$

$$\frac{6x}{6} = \frac{24}{6}$$

$$x = \frac{24}{6}$$

$$x = 4$$

h) $\frac{2}{5}m = 10$

$$\frac{2m}{5} \times 5 = 10 \times 5$$

$$2m = 50$$

$$m = \frac{50}{2}$$

$$m = 25$$

i) $\frac{3m}{4} = -6$

$$\frac{3m}{4} \times 4 = -6 \times 4$$

$$3m = -24$$

$$m = \frac{-24}{3}$$

$$m = -8$$

Solve the following equations

3 a) $2x - 1 = 9$

$2x - 1 + 1 = 9 + 1$ ✓

$\frac{2x}{2} = \frac{10}{2}$ ✓

$x = 5$ ✓

b) $5(2 - x) - 3(4 - 2x) = 20$

$10 - 5x - 12 + 6x = 20$ ✓

$10 - 5x + 6x - 12 = 20$ ✓

$10 - 12 - 5x + 6x = 20$

$-2 + x = 20$ ✓

$-2 + 2 + x = 20 + 2$ ✓

$x = 22$

c) $2m + 4 - 3m = 8(m - 1)$

$2m + 4 - 3m = 8m - 8$

$2m - 3m + 4 = 8m - 8$ ✓

$-m + 4 = 8m - 8$ ✓

$-m - 8m = -8 - 4$ ✓

$\frac{-9m}{-9} = \frac{-12}{-9}$

$m = \frac{-12}{-9}$

$m = \frac{4}{3}$ ✓

Simplify!

d) $\frac{x+1}{4} = 5$

$\frac{x+1}{4} \times 4 = 5 \times 4$

$x+1 = 20$ ✓

$x+1 = 20$ ✓

$x+1-1 = 20-1$ ✓

$x = 19$ ✓

e) $\frac{x}{5} + \frac{x}{3} = 10$

$$\begin{array}{r} 5 \overline{) 5, 3} \\ 3 \overline{) 1, 3} \\ \underline{1, 1} \end{array}$$

$\frac{3x}{15} + \frac{5x}{15} = 10$ ✓

$\frac{3x + 5x}{15} = 10$ ✓

$\frac{8x}{15} = \frac{150}{15}$ ✓

$1(8x) = 10(15)$

$\frac{8x}{8} = \frac{150}{8}$ ✓

$x = \frac{75}{4}$ ✓

$x = 18.75$

$x = 18\frac{3}{4}$

$$\begin{array}{r} 18 \\ 4 \overline{) 75} \\ \underline{32} \\ 3 \end{array}$$

$$f) 5(y+2) - 4(y-1) = 6$$

$$5y + 10 - 4y + 4 = 6 \quad \checkmark$$

$$5y - 4y + 10 + 4 = 6 \quad \checkmark$$

$$y + 14 = 6 \quad \checkmark$$

$$y + 14 - 14 = 6 - 14 \quad \checkmark$$

$$y = -8 \quad \checkmark$$

$$g) 4(y+3) - 2y = 7$$

$$4y + 12 - 2y = 7 \quad \checkmark$$

$$4y - 2y + 12 = 7 \quad \checkmark$$

$$2y + 12 = 7 \quad \checkmark$$

$$2y + 12 - 12 = 7 - 12$$

$$\frac{2y}{2} = \frac{-5}{2} \quad \checkmark$$

$$y = \frac{-5}{2} \quad \checkmark$$

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4) Solve each of the following simultaneous equations by using (a) elimination method and (b) substitution method.

a) $3u + v = 15$; $3u + 2v = 10$

$$\begin{array}{r} 3u + v = 15 \quad \text{---} \quad (1) \\ -) \quad 3u + 2v = 10 \quad \text{---} \quad (2) \\ \hline -v = 5 \end{array}$$

$+v = 5$
 $\hline$
 $\text{Then, } v = -5$

$v = -5$

Substitute $-v = 5$ into (2)

$3u + 2(5) = 10$

$3u + 10 = 10$

$3u + 10 - 10 = 10 - 10$

$\frac{3u}{3} = \frac{0}{3}$

$u = 0$

$\therefore u = 0, v = 5$

$3u + 2(-5) = 10$

$3u - 10 = 10$

$3u = 10 + 10$

$3u = 20$

$u = \frac{20}{3}$

$\therefore u = \frac{20}{3}, v = -5$

Please try again.

b) Substitution method

$$3u + v = 15 \quad \text{--- (1)}$$

$$3u + 2v = 10 \quad \text{--- (2)}$$

From (2), $3u + 2v = 10$ ✓

$$3u + 2v - 2v = 10 - 2v \quad \checkmark$$

$$\frac{3u}{3} = \frac{10 - 2v}{3} \quad \checkmark$$

$$u = \frac{10 - 2v}{3} \quad \checkmark \quad \text{--- (3)}$$

Substitute (3) into (1)

$$3\left(\frac{10 - 2v}{3}\right) + v = 15 \quad \checkmark$$

$$(10 - 2v) + v = 15 \quad \checkmark$$

$$10 - 2v + v = 15 \quad \checkmark$$

$$10 - v = 15 \quad \checkmark$$

$$10 - 10 - v = 15 - 10 \quad \checkmark$$

$$v = 5 \quad \checkmark$$

$$-v = 5$$

$$v = -5$$

Substitute $v = -5$ into (2)

$$3u + 2(-5) = 10$$

$$3u + 10 = 10$$

$$3u + 10 - 10 = 10 - 10$$

$$\frac{3u}{3} = \frac{0}{3}$$

$$u = 0$$

$$3u + 2(-5) = 10$$

$$3u - 10 = 10$$

$$3u = 20$$

$$u = \frac{20}{3}$$

$$\therefore u = 0 \quad v = 5$$

$$b) 2a + 2x = 18 ; a + 2x = 17$$

$$2a + 2x = 18$$

①

$$a + 2x = 17$$

②

a) Elimination method :

$$2a + 2x = 18$$

$$-) \quad a + 2x = 17$$

$$a = 1$$

$$a = 1 *$$

Substitute $a = 1$ into ①

$$2(1) + 2x = 18$$

$$2 + 2x = 18$$

$$2 - 2 + 2x = 18 - 2$$

$$\frac{2x}{2} = \frac{16}{2}$$

$$x = \frac{16}{2}$$

$$x = 8 *$$

$$\therefore a = 1, x = 8$$

$$31 = x + a \quad [-1] \times ① + ② = 0$$

$$2 - (1)$$

$$2 - 1$$

$$1$$

$$① \times (-1) = 0 \text{ substitute}$$

$$31 = x + a \quad (-1) \times$$

$$31 = x + a$$

$$-31 = -x - a$$

$$31 = x$$

$$31 = x$$

$$31 = x$$

$$1 \times$$

$$8 = x$$

$$3 = x, 1 = a \therefore$$

b) Substitution method :

$$2a + 2x = 18 \quad \text{--- (1)}$$

$$a + 2x = 17 \quad \text{--- (2)}$$

$$31 = x + 20$$

$$x = 11$$

From (1), $2a + 2x = 18$

$$2a - 2a + 2x = 18 - 2a$$

$$\frac{2x}{2} = \frac{18 - 2a}{2}$$

$$x = \frac{18 - 2a}{2}$$

$$x = \frac{18 - 2a}{2}$$

$$x = 1$$

bottam bottamilla (0)

$$31 = x + 20$$

$$x = 11$$

$$1 = 11$$

$$(3)$$

$$1 = 11$$

Substitute (3) into (2)

$$a + \frac{18 - 2a}{2} = 17$$

$$a + 18 - 2a = 17$$

$$-a + 18 = 17$$

$$-a + 18 - 18 = 17 - 18$$

$$-a = -1$$

$$+1 \quad +1$$

$$a = 1$$

(1) into 1 = 11 substitute

$$31 = x + 20$$

$$31 = x + 20$$

$$31 - 20 = x + 20 - 20$$

$$11 = x$$

$$x = 11$$

$$31 = x$$

$$11 = x$$

$$x = 11$$

$$3 = x, 1 = 11$$

Substitute $a = 1$ into (1)

$$2(1) + 2x = 18$$

$$2 + 2x = 18$$

$$2 - 2 + 2x = 18 - 2$$

$$\frac{2x}{2} = \frac{16}{2}$$

$$x = \frac{16}{2}$$

$$x = 8$$

$$\therefore a = 1, x = 8$$

$$c) -5x + 5y = 0 ; -5x + 3y = 8$$

a) Elimination method:

$$-5x + 5y = 0 \quad \text{--- (1)}$$

$$\rightarrow -5x + 3y = 8 \quad \text{--- (2)}$$

$$\frac{2y}{2} = \frac{-8}{2}$$

$$y = \frac{-8}{2} = -4$$

$$y = -4$$

Substitute $y = -4$ into (2)

$$-5x + 3(-4) = 8$$

$$-5x - 12 = 8$$

$$-5x - 12 + 12 = 8 + 12$$

$$\frac{-5x}{-5} = \frac{20}{-5}$$

$$x = \frac{20}{-5}$$

$$x = -4$$

$$\therefore x = -4, y = -4$$

b) Substitution method

$$-5x + 5y = 0 \quad \text{--- (1)}$$

$$-5x + 3y = 8 \quad \text{--- (2)}$$

From (2) $-5x + 3y = 8$

$$-5x + 3y - 3y = 8 - 3y$$

$$\frac{-5x}{-5} = \frac{8-3y}{-5}$$

$$x = \frac{8-3y}{-5} \quad \text{--- (3)}$$

Substitute (3) into (1)

$$-5\left(\frac{8-3y}{-5}\right) + 5y = 0$$

$$(8-3y) + 5y = 0$$

$$8 - 3y + 5y = 0$$

$$8 - 2y = 0$$

$$8 - 8 - 2y = 0 - 8$$

$$\frac{2y}{2} = \frac{-8-4}{2}$$

$$y = -4$$

Substitute $y = -4$ into (2)

$$-5x + 3(-4) = 8$$

$$-5x - 12 = 8$$

$$-5x - 12 + 12 = 8 + 12$$

$$\frac{-5x}{-5} = \frac{20-4}{-5}$$

$$x = -4$$

$$\therefore x = -4, y = -4$$

$$d) 7x + 9y = 27 ; 9x + 9y = 27$$

a) Elimination method :

$$7x + 9y = 27 \quad \text{--- (1)}$$

$$-) \quad 9x + 9y = 27 \quad \text{--- (2)}$$

$$\frac{-7x}{-2} = \frac{0}{-2}$$

$$x = \frac{0}{2}$$

$$x = 0$$

Substitute $x = 0$ into (1)

$$7(0) + 9y = 27$$

$$\frac{9y}{9} = \frac{27}{9}$$

$$y = \frac{27}{9}$$

$$y = 3$$

$$\therefore x = 0, y = 3$$

$$FC = yP + xF$$

$$FC = yP + xP$$

$$FC = yP + xP \quad \text{(c) mod}$$

$$yP - FC = yP - yP + xP$$

$$yP - FC = xP$$

$$yP - FC = x$$

$$\text{(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13) (14) (15) (16) (17) (18) (19) (20) (21) (22) (23) (24) (25) (26) (27) (28) (29) (30) (31) (32) (33) (34) (35) (36) (37) (38) (39) (40) (41) (42) (43) (44) (45) (46) (47) (48) (49) (50) (51) (52) (53) (54) (55) (56) (57) (58) (59) (60) (61) (62) (63) (64) (65) (66) (67) (68) (69) (70) (71) (72) (73) (74) (75) (76) (77) (78) (79) (80) (81) (82) (83) (84) (85) (86) (87) (88) (89) (90) (91) (92) (93) (94) (95) (96) (97) (98) (99) (100)$$

$$FC = yP + (yP - FC)P$$

$$FC = yP + (yP - FC)P$$

$$FC = yP + yP - FC$$

$$FC = FC$$

$$FC - FC = FC - FC$$

$$0 = 0$$

$$\text{(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13) (14) (15) (16) (17) (18) (19) (20) (21) (22) (23) (24) (25) (26) (27) (28) (29) (30) (31) (32) (33) (34) (35) (36) (37) (38) (39) (40) (41) (42) (43) (44) (45) (46) (47) (48) (49) (50) (51) (52) (53) (54) (55) (56) (57) (58) (59) (60) (61) (62) (63) (64) (65) (66) (67) (68) (69) (70) (71) (72) (73) (74) (75) (76) (77) (78) (79) (80) (81) (82) (83) (84) (85) (86) (87) (88) (89) (90) (91) (92) (93) (94) (95) (96) (97) (98) (99) (100)$$

$$FC = yP + (0)P$$

$$FC = yP$$

$$yP - FC = yP - yP = 0$$

$$\text{(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (13) (14) (15) (16) (17) (18) (19) (20) (21) (22) (23) (24) (25) (26) (27) (28) (29) (30) (31) (32) (33) (34) (35) (36) (37) (38) (39) (40) (41) (42) (43) (44) (45) (46) (47) (48) (49) (50) (51) (52) (53) (54) (55) (56) (57) (58) (59) (60) (61) (62) (63) (64) (65) (66) (67) (68) (69) (70) (71) (72) (73) (74) (75) (76) (77) (78) (79) (80) (81) (82) (83) (84) (85) (86) (87) (88) (89) (90) (91) (92) (93) (94) (95) (96) (97) (98) (99) (100)$$

$$FC = yP + (0)P$$

$$FC = yP$$

$$yP - FC = yP - yP = 0$$

$$0 = 0$$

b) Substitution method

$$7x + 9y = 27 \quad \text{--- ①}$$

$$9x + 9y = 27 \quad \text{--- ②}$$

From ②

$$9x + 9y = 27$$

$$9x + 9y - 9y = 27 - 9y$$

$$\frac{9x}{9} = \frac{27 - 9y}{9}$$

$$x = \frac{27 - 9y}{9} \quad \text{--- ③}$$

Substitute ③ into ①

$$7\left(\frac{27 - 9y}{9}\right) + 9y = 27$$

$$(27 - 9y) + 9y = 27$$

$$27 - 9y + 9y = 27$$

$$27 = 27$$

$$27 - 27 = 27 - 27$$

$$x = 0$$

Substitute $x = 0$ into ①

$$7(0) + 9y = 27$$

$$9y = 27$$

$$9y + 9y = 9y - 9y = 27 - 9y$$

$$y =$$

Substitute $x = 0$ into ①

$$7(0) + 9y = 27$$

$$\frac{9y}{9} = \frac{27}{9}$$

$$y = \frac{27}{9}$$

$$y = 3$$

$$\therefore x = 0, y = 3$$