

### Worksheet 13

#### Mathematical Recursion

1. The Fibonacci numbers  $f_0, f_1, f_2, \dots$  are defined by the equations  $f(0) = f(1) = 1$  and  $f(n + 1) = f(n)^2 + f(n - 1)^3$  for  $n = 1, 2, 3, \dots$ . Identify  $f(2)$ ,  $f(3)$  and  $f(4)$ .
2. Find the first 5 terms for the given sequences.
  - (a)  $a_n = \frac{n}{2}, n = 1, 2, 3, \dots$
  - (b)  $b_n = \frac{1 + (-1)^n}{2}, n \geq 1$